

# BCA SEMESTER 2 — STATISTICS (Complete Notes)

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## UNIT 1: INTRODUCTION TO STATISTICS

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### 1.1 Definition of Statistics

**Statistics** (Plural sense): Numerical facts collected in a systematic manner. **Statistics** (Singular sense): The science of collecting, organizing, analyzing, interpreting, and presenting data.

**Croxton and Cowden:** "Statistics is the science which deals with collection, analysis and interpretation of numerical data."

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### 1.2 Types of Data

#### A. Primary Data

Data collected **first-hand** by the investigator for a specific purpose.

##### Methods of collection:

- Direct personal interview
- Indirect oral investigation
- Questionnaire method
- Schedule method
- Observation method

#### B. Secondary Data

Data collected by **someone else** and used by the investigator.

##### Sources:

- Government publications
- Journals, newspapers
- Websites, databases

## Difference Table

Feature	Primary Data	Secondary Data
Originality	Original	Already collected
Cost	Expensive	Economical
Time	Time-consuming	Quick
Reliability	More reliable	Less reliable
Suitability	Specific purpose	May not fit exactly

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## 1.3 Classification of Data

**Classification** = Arranging data into groups based on similarities.

### Types:

1. **Geographical** – By location (state, city)
  2. **Chronological/Temporal** – By time (year, month)
  3. **Qualitative** – By attributes (gender, religion)
  4. **Quantitative** – By numerical values (income, marks)
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## 1.4 Tabulation

**Tabulation** = Systematic arrangement of data in rows and columns.

### Parts of a Table:

- Table number
  - Title
  - Column headings (caption)
  - Row headings (stub)
  - Body of the table
  - Footnotes
  - Source
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## 1.5 Frequency Distribution

**Frequency** = Number of times a value occurs.

### Types:

1. **Ungrouped (Discrete) Frequency Distribution**
2. **Grouped (Continuous) Frequency Distribution**

### Key Terms:

- **Class Interval:** Range of values in a class (e.g., 10–20)
- **Class Width:** Upper limit – Lower limit = 20 – 10 = 10
- **Class Mark (Mid-value):** (Lower limit + Upper limit) / 2
- **Cumulative Frequency:** Running total of frequencies

**Example:****Marks Frequency (f) Cumulative Frequency (CF)**

0–10	5	5
10–20	8	13
20–30	12	25
30–40	10	35
40–50	5	40

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**1.6 Diagrammatic & Graphical Representation****Diagrams:**

- **Bar Diagram** (Simple, Multiple, Subdivided)
- **Pie Chart** (Circle divided into sectors)

**Graphs:**

- **Histogram** – For continuous data (bars touching)
- **Frequency Polygon** – Join mid-points of histogram tops
- **Ogive (Cumulative Frequency Curve)** – Less than / More than type
- **Frequency Curve** – Smooth version of frequency polygon

**Pie Chart Formula:**

$$\text{Angle of sector} = (\text{Component Value} / \text{Total Value}) \times 360^\circ$$

**Example:** If expenditure on food = 400 out of total 2000

$$\text{Angle} = (400/2000) \times 360^\circ = 72^\circ$$


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**UNIT 2: MEASURES OF CENTRAL TENDENCY**

## 2.1 Introduction

A **Measure of Central Tendency** is a single value that represents the center of the data.

### Properties of a Good Average:

1. Rigidly defined
2. Easy to understand and compute
3. Based on all observations
4. Capable of further algebraic treatment
5. Not affected much by extreme values

## 2.2 Arithmetic Mean (AM)

### A. For Raw Data (Ungrouped):

$$\bar{x} = \frac{\sum x}{n}$$

**Example:** Find mean of 5, 10, 15, 20, 25

$$\bar{x} = (5 + 10 + 15 + 20 + 25) / 5 = 75/5 = 15$$

### B. For Discrete Frequency Distribution:

$$\bar{x} = \frac{\sum f x}{\sum f}$$

**Example:**

**x** 10 20 30 40 50

**f** 3 5 7 4 1

$$\sum fx = 30 + 100 + 210 + 160 + 50 = 550$$

$$\sum f = 20$$

$$\bar{x} = 550/20 = 27.5$$

### C. For Grouped (Continuous) Data:

**Direct Method:**

$$\bar{x} = \frac{\sum f m}{\sum f} \quad (\text{where } m = \text{mid-value of class})$$

**Shortcut (Assumed Mean) Method:**

$$\bar{x} = A + (\sum f d / \sum f) \quad \text{where } d = m - A$$

**Step Deviation Method:**

$$\bar{x} = A + (\sum f u / \sum f) \times h \quad \text{where } u = (m - A)/h$$

**Solved Example (Step Deviation):**

**Class**   **f**   **Mid (m)**   **u = (m-25)/10**   **fu**

0-10	5	5	-2	-10
10-20	8	15	-1	-8
20-30	12	25	0	0
30-40	10	35	1	10
40-50	5	45	2	10

$$A = 25, h = 10, \sum f = 40, \sum fu = 2$$

$$\bar{x} = 25 + (2/40) \times 10 = 25 + 0.5 = 25.5$$

**Combined Mean:**

$$\bar{x}_{12} = (n_1\bar{x}_1 + n_2\bar{x}_2) / (n_1 + n_2)$$

**Weighted Mean:**

$$\bar{x}_w = \sum w \cdot x / \sum w$$

**Properties of Arithmetic Mean:**

1.  $\sum(x - \bar{x}) = 0$  (sum of deviations from mean is zero)
2.  $\sum(x - \bar{x})^2$  is minimum
3. If each value is multiplied by k, new mean =  $k \times \bar{x}$
4. If constant c is added to each value, new mean =  $\bar{x} + c$

## 2.3 Median

**Median** = The middle value when data is arranged in ascending/descending order.

**A. For Raw Data:**

Arrange in order. If n is odd:

$$\text{Median} = ((n+1)/2)\text{th value}$$

If  $n$  is even:

Median = Average of  $(n/2)$ th and  $(n/2 + 1)$ th values

**Example (Odd):** 3, 5, 7, 9, 11  $n = 5$

Median =  $(5+1)/2 = 3$ rd value = 7

**Example (Even):** 2, 4, 6, 8  $n = 4$

Median =  $(4/2)$ th +  $(4/2+1)$ th / 2 =  $(2\text{nd} + 3\text{rd})/2 = (4+6)/2 = 5$

## B. For Discrete Frequency Distribution:

Find cumulative frequency. Median = value corresponding to  $CF \geq N/2$ .

## C. For Grouped Data:

Median =  $L + [(N/2 - CF) / f] \times h$

Where:

- $L$  = Lower limit of median class
- $N$  = Total frequency ( $\Sigma f$ )
- $CF$  = Cumulative frequency of class preceding median class
- $f$  = Frequency of median class
- $h$  = Class width

### Solved Example:

**Class f CF**

0-10 5 5

10-20 8 13

20-30 12 25

30-40 10 35

40-50 5 40

$N = 40$ ,  $N/2 = 20$

Median class = 20-30 (CF just  $\geq 20$ )

$L = 20$ ,  $CF = 13$ ,  $f = 12$ ,  $h = 10$

Median =  $20 + [(20-13)/12] \times 10$

=  $20 + (7/12) \times 10$

=  $20 + 5.83$

= 25.83

## 2.4 Mode

**Mode** = The value that occurs most frequently.

### A. For Raw Data:

Simply find the most repeated value.

**Example:** 2, 3, 5, 5, 5, 7, 8    Mode = 5

### B. For Grouped Data:

$$\text{Mode} = L + \left[ \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right] \times h$$

Where:

- L = Lower limit of modal class (class with highest frequency)
- $f_1$  = Frequency of modal class
- $f_0$  = Frequency of class preceding modal class
- $f_2$  = Frequency of class succeeding modal class
- h = Class width

### Solved Example:

#### Class f

0-10	5
10-20	8
20-30	12
30-40	10
40-50	5

$$\begin{aligned} L &= 20, f_1 = 12, f_0 = 8, f_2 = 10, h = 10 \\ \text{Mode} &= 20 + \left[ \frac{12-8}{2 \times 12 - 8 - 10} \right] \times 10 \\ &= 20 + \left[ \frac{4}{6} \right] \times 10 \\ &= 20 + 6.67 \\ &= 26.67 \end{aligned}$$

## 2.5 Empirical Relationship

$$\text{Mode} = 3 \text{ Median} - 2 \text{ Mean}$$

or equivalently:

$$\text{Mean} - \text{Mode} = 3(\text{Mean} - \text{Median})$$

## 2.6 Geometric Mean (GM)

### For Raw Data:

$$GM = (x_1 \cdot x_2 \cdot x_3 \cdot \dots \cdot x_n)^{(1/n)}$$

or equivalently:

$$\log(GM) = (1/n) \sum \log(x_i)$$

### For Frequency Distribution:

$$\log(GM) = \frac{\sum f_i \log(x_i)}{\sum f_i}$$

**Example:** Find GM of 2, 4, 8

$$GM = (2 \times 4 \times 8)^{(1/3)} = (64)^{(1/3)} = 4$$

**Use:** Best for rates of growth, ratios, percentages.

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## 2.7 Harmonic Mean (HM)

### For Raw Data:

$$HM = n / \sum (1/x_i)$$

### For Frequency Distribution:

$$HM = \frac{\sum f_i}{\sum (f_i / x_i)}$$

**Example:** Find HM of 2, 4, 8

$$HM = 3 / (1/2 + 1/4 + 1/8) = 3 / (0.5 + 0.25 + 0.125) = 3/0.875 = 3.43$$

**Use:** Best for speed, rates (time-based problems).

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## 2.8 Relationship Between AM, GM, HM

$$AM \geq GM \geq HM \quad (\text{for positive values})$$

Also:

$$GM^2 = AM \times HM$$

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## 2.9 Quartiles, Deciles, and Percentiles

**Quartiles (divide data into 4 parts):**

$$Q_1 = L + [(N/4 - CF)/f] \times h$$

$Q_2 = \text{Median}$

$$Q_3 = L + [(3N/4 - CF)/f] \times h$$

**Deciles (divide data into 10 parts):**

$$D_k = L + [(kN/10 - CF)/f] \times h \quad (k = 1, 2, \dots, 9)$$

**Percentiles (divide data into 100 parts):**

$$P_k = L + [(kN/100 - CF)/f] \times h \quad (k = 1, 2, \dots, 99)$$

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# UNIT 3: MEASURES OF DISPERSION

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## 3.1 Introduction

**Dispersion** measures the **spread or variability** of data around the central value.

**Types:**

1. **Absolute Measures:** Range, QD, MD, SD
  2. **Relative Measures:** Coefficient of Range, Coefficient of QD, Coefficient of MD, Coefficient of Variation (CV)
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## 3.2 Range

$$\begin{aligned} \text{Range} &= \text{Maximum Value} - \text{Minimum Value} \\ &= L - S \end{aligned}$$

$$\text{Coefficient of Range} = (L - S) / (L + S)$$

**Example:** Data: 5, 10, 15, 20, 25

$$\begin{aligned} \text{Range} &= 25 - 5 = 20 \\ \text{Coefficient of Range} &= (25-5)/(25+5) = 20/30 = 0.667 \end{aligned}$$

### 3.3 Quartile Deviation (Semi-Interquartile Range)

$$\text{QD} = (Q_3 - Q_1) / 2$$

$$\text{Coefficient of QD} = (Q_3 - Q_1) / (Q_3 + Q_1)$$

**Example:** If  $Q_1 = 20$ ,  $Q_3 = 40$

$$\begin{aligned} \text{QD} &= (40-20)/2 = 10 \\ \text{Coefficient of QD} &= (40-20)/(40+20) = 20/60 = 0.333 \end{aligned}$$

### 3.4 Mean Deviation (Average Deviation)

**About Mean:**

$$\begin{aligned} \text{MD}(\bar{x}) &= \sum |x - \bar{x}| / n && \text{(Raw data)} \\ \text{MD}(\bar{x}) &= \sum f |x - \bar{x}| / \sum f && \text{(Frequency distribution)} \end{aligned}$$

**About Median:**

$$\text{MD}(\text{Median}) = \sum |x - \text{Median}| / n$$

$$\text{Coefficient of MD} = \text{MD} / \text{Mean (or Median)}$$

**Solved Example:** Find MD about mean for: 2, 4, 6, 8, 10

$$\bar{x} = (2+4+6+8+10)/5 = 30/5 = 6$$

$$|2-6| + |4-6| + |6-6| + |8-6| + |10-6|$$

$$= 4 + 2 + 0 + 2 + 4 = 12$$

$$MD = 12/5 = 2.4$$

$$\text{Coefficient of MD} = 2.4/6 = 0.4$$

### 3.5 Standard Deviation ( $\sigma$ ) and Variance ( $\sigma^2$ )

**Standard Deviation** is the most important and widely used measure of dispersion.

#### A. For Raw Data:

##### Direct Method:

$$\sigma = \sqrt{[\sum(x - \bar{x})^2 / n]}$$

##### Shortcut Method:

$$\begin{aligned} \sigma &= \sqrt{[(\sum x^2/n) - (\sum x / n)^2]} \\ &= \sqrt{[(\sum x^2/n) - \bar{x}^2]} \end{aligned}$$

#### B. For Discrete Frequency Distribution:

$$\sigma = \sqrt{[(\sum f x^2 / \sum f) - (\sum f x / \sum f)^2]}$$

#### C. For Grouped Data (Step Deviation):

$$\sigma = h \times \sqrt{[(\sum f u^2 / N) - (\sum f u / N)^2]}$$

where  $u = (m - A)/h$ ,  $N = \sum f$

#### Variance:

$$\text{Variance } (\sigma^2) = (\text{Standard Deviation})^2$$

#### Solved Example (Raw Data):

Find  $\sigma$  for: 4, 6, 8, 10, 12

$$\bar{x} = (4+6+8+10+12)/5 = 40/5 = 8$$

$$\begin{aligned} &(4-8)^2 + (6-8)^2 + (8-8)^2 + (10-8)^2 + (12-8)^2 \\ &= 16 + 4 + 0 + 4 + 16 = 40 \end{aligned}$$

$$\sigma^2 = 40/5 = 8$$

$$\sigma = \sqrt{8} = 2.83$$

### Solved Example (Grouped Data):

Class	f	m	u=(m-25)/10	fu	fu <sup>2</sup>
0-10	5	5	-2	-10	20
10-20	8	15	-1	-8	8
20-30	12	25	0	0	0
30-40	10	35	1	10	10
40-50	5	45	2	10	20
<b>Total</b>	<b>40</b>			<b>2</b>	<b>58</b>

$$\begin{aligned}\sigma &= h \times \sqrt{[(\sum fu^2/N) - (\sum fu/N)^2]} \\ &= 10 \times \sqrt{[(58/40) - (2/40)^2]} \\ &= 10 \times \sqrt{[1.45 - 0.0025]} \\ &= 10 \times \sqrt{1.4475} \\ &= 10 \times 1.203 \\ &= 12.03\end{aligned}$$

## 3.6 Properties of Standard Deviation

1.  $\sigma$  is always **non-negative** ( $\sigma \geq 0$ )
2. If all values are same,  $\sigma = 0$
3.  $\sigma$  is **independent of change of origin** (adding constant doesn't change  $\sigma$ )
4.  $\sigma$  is **dependent on change of scale** (multiplying by  $k$  gives new  $\sigma = |k|\sigma$ )
5. **Combined SD** of two groups:

$$\sigma_{12}^2 = (n_1(\sigma_1^2 + d_1^2) + n_2(\sigma_2^2 + d_2^2)) / (n_1 + n_2)$$

where  $d_1 = \bar{x}_1 - \bar{x}_{12}$ ,  $d_2 = \bar{x}_2 - \bar{x}_{12}$

## 3.7 Coefficient of Variation (CV)

$$CV = (\sigma / \bar{x}) \times 100 \%$$

**Use:** Comparing variability of two or more distributions.

**The distribution with smaller CV is more consistent/uniform.**

**Example:**

- Group A:  $\bar{x} = 50$ ,  $\sigma = 10$      $CV = (10/50) \times 100 = 20\%$

- Group B:  $\bar{x} = 60, \sigma = 15$   $CV = (15/60) \times 100 = 25\%$

**Group A is more consistent** (lower CV).

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## 3.8 Relationship between Measures of Dispersion

$$QD = (2/3) \times SD \quad (\text{approximately})$$

$$MD = (4/5) \times SD \quad (\text{approximately})$$

More precisely:

$$4 SD = 5 MD = 6 QD \quad (\text{approximately})$$

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# UNIT 4: SKEWNESS AND KURTOSIS

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## 4.1 Skewness

**Skewness** measures the **asymmetry** of a frequency distribution.

**Types:**

1. **Symmetrical Distribution:** Mean = Median = Mode, Skewness = 0
  2. **Positively Skewed:** Mean > Median > Mode (tail extends to right)
  3. **Negatively Skewed:** Mean < Median < Mode (tail extends to left)
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## 4.2 Measures of Skewness

**A. Karl Pearson's Coefficient of Skewness:**

$$Sk_p = (\text{Mean} - \text{Mode}) / \sigma$$

or (when mode is ill-defined):

$$Sk_p = 3(\text{Mean} - \text{Median}) / \sigma$$

**Range:** Usually between -3 and +3

### B. Bowley's Coefficient of Skewness:

$$Sk = (Q_3 + Q_1 - 2Q_2) / (Q_3 - Q_1)$$

where  $Q_2 = \text{Median}$

**Range:**  $-1 \leq Sk \leq +1$

### C. Kelly's Coefficient of Skewness:

$$Sk_k = (P_{90} + P_{10} - 2P_{50}) / (P_{90} - P_{10})$$

### Solved Example:

Given: Mean = 45, Median = 40,  $\sigma = 10$

$$Sk_p = 3(45 - 40)/10 = 15/10 = 1.5 \text{ (Positively Skewed)}$$

## 4.3 Moments

### Raw Moments (about origin):

$$\mu^r = \sum x^r / n \quad (\text{raw data})$$

$$\mu^r = \sum f x^r / \sum f \quad (\text{frequency distribution})$$

- $\mu^1 = \text{Mean}$
- $\mu^2 = \sum x^2 / n$

### Central Moments (about mean):

$$\mu_r = \sum (x - \bar{x})^r / n$$

- $\mu_1 = 0$  (always)
- $\mu_2 = \text{Variance} = \sigma^2$
- $\mu_3 = \text{Used for skewness}$
- $\mu_4 = \text{Used for kurtosis}$

### Relationship between Central and Raw Moments:

$$\mu_1 = 0$$

$$\mu_2 = \mu^2 - (\mu^1)^2$$

$$\mu_3 = \mu'_3 - 3\mu'_2\mu'_1 + 2(\mu'_1)^3$$

$$\mu_4 = \mu'_4 - 4\mu'_3\mu'_1 + 6\mu'_2(\mu'_1)^2 - 3(\mu'_1)^4$$

## 4.4 Skewness using Moments

**Karl Pearson's  $\beta_1$  and  $\gamma_1$ :**

$$\beta_1 = \mu_3^2 / \mu_2^3$$

$$\gamma_1 = \sqrt{\beta_1} = \mu_3 / \mu_2^{3/2}$$

- If  $\gamma_1 = 0$  Symmetrical
- If  $\gamma_1 > 0$  Positively skewed
- If  $\gamma_1 < 0$  Negatively skewed

## 4.5 Kurtosis

**Kurtosis** measures the **peakedness** or **flatness** of a distribution.

**Karl Pearson's  $\beta_2$  and  $\gamma_2$ :**

$$\beta_2 = \mu_4 / \mu_2^2$$

$$\gamma_2 = \beta_2 - 3$$

**Types:**

1. **Mesokurtic:**  $\beta_2 = 3$ ,  $\gamma_2 = 0$  (Normal distribution)
2. **Leptokurtic:**  $\beta_2 > 3$ ,  $\gamma_2 > 0$  (More peaked, heavier tails)
3. **Platykurtic:**  $\beta_2 < 3$ ,  $\gamma_2 < 0$  (Flatter, lighter tails)

**Solved Example on Moments:**

Find first four central moments and  $\beta_1$ ,  $\beta_2$  for:

**x 2 3 4 5 6**

**f 1 3 5 3 1**

$$N = 13, \bar{x} = \sum fx / N = (2+9+20+15+6) / 13 = 52 / 13 = 4$$

$$\mu_2 = \sum f(x-\bar{x})^2 / N = [1(4)+3(1)+5(0)+3(1)+1(4)] / 13 = 10 / 13 = 0.769$$

$$\mu_3 = \sum f(x-\bar{x})^3 / N = [1(-8)+3(-1)+5(0)+3(1)+1(8)] / 13 = 0 / 13 = 0$$

$$\mu_4 = \sum f(x-\bar{x})^4 / N = [1(16)+3(1)+5(0)+3(1)+1(16)] / 13 = 36 / 13 = 2.769$$

$$\beta_1 = \mu_3^2/\mu_2^3 = 0/(0.769)^3 = 0 \quad \text{Symmetrical}$$
$$\beta_2 = \mu_4/\mu_2^2 = 2.769/(0.769)^2 = 2.769/0.591 = 4.68 \quad \text{Leptokurtic}$$

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## UNIT 5: CORRELATION ANALYSIS

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### 5.1 Introduction

**Correlation** measures the **degree and direction of linear relationship** between two variables.

**Types:**

1. **Positive Correlation:** Both variables move in same direction
2. **Negative Correlation:** Variables move in opposite directions
3. **Zero Correlation:** No linear relationship

**Degree:**

- **Perfect:**  $r = +1$  or  $r = -1$
  - **High:**  $0.75 < |r| < 1$
  - **Moderate:**  $0.25 < |r| < 0.75$
  - **Low:**  $0 < |r| < 0.25$
  - **No correlation:**  $r = 0$
- 

### 5.2 Scatter Diagram

A **scatter diagram** is a graph of plotted points showing the relationship between two variables.

- Points close to a line    High correlation
  - Points scattered    Low correlation
  - Upward trend    Positive correlation
  - Downward trend    Negative correlation
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### 5.3 Karl Pearson's Coefficient of Correlation (r)

**Formula:**

$$r = \frac{\sum(x - \bar{x})(y - \bar{y})}{\sqrt{[\sum(x - \bar{x})^2 \times \sum(y - \bar{y})^2]}}$$

**Shortcut Formula:**

$$r = \frac{[n\sum xy - \sum x \sum y]}{\sqrt{[n\sum x^2 - (\sum x)^2][n\sum y^2 - (\sum y)^2]}}$$

**Range:**  $-1 \leq r \leq +1$ **Solved Example:****x** 1 2 3 4 5**y** 2 4 5 4 5

$$n = 5$$

$$\sum x = 15, \sum y = 20$$

$$\sum x^2 = 1+4+9+16+25 = 55$$

$$\sum y^2 = 4+16+25+16+25 = 86$$

$$\sum xy = 2+8+15+16+25 = 66$$

$$\begin{aligned} r &= \frac{[5(66) - 15(20)]}{\sqrt{[5(55) - (15)^2][5(86) - (20)^2]}} \\ &= \frac{[330 - 300]}{\sqrt{[275 - 225][430 - 400]}} \\ &= \frac{30}{\sqrt{50 \times 30}} \\ &= \frac{30}{\sqrt{1500}} \\ &= \frac{30}{38.73} \\ &= 0.775 \end{aligned}$$

**Interpretation:** High positive correlation.

## 5.4 Properties of Correlation Coefficient

1.  $-1 \leq r \leq +1$
2.  $r$  is dimensionless (unit-free)
3.  $r$  is independent of change of origin and scale
4.  $r(x,y) = r(y,x)$  (symmetric)
5. If  $r = 0$ , variables are uncorrelated (not necessarily independent)
6.  $r$  measures only **linear** relationship

## 5.5 Spearman's Rank Correlation Coefficient ( $\rho$ )

Used when data is in **ranks** or **ordinal** form.**When ranks are NOT repeated:**

$$\rho = 1 - [6\sum D^2 / n(n^2-1)]$$

where  $D = \text{Rank of } x - \text{Rank of } y$

### When ranks are REPEATED:

$$\rho = 1 - [6(\sum D^2 + CF) / n(n^2-1)]$$

where  $CF = \sum[(m^3-m)/12]$  for each repeated rank ( $m = \text{number of times repeated}$ )

### Solved Example (No Repeat):

Student Rank in Math ( $R_1$ ) Rank in Stats ( $R_2$ )  $D = R_1 - R_2$   $D^2$

A	1	2	-1	1
B	2	1	1	1
C	3	3	0	0
D	4	5	-1	1
E	5	4	1	1

$$n = 5, \sum D^2 = 4$$

$$\rho = 1 - [6(4) / 5(25-1)]$$

$$= 1 - [24/120]$$

$$= 1 - 0.2$$

$$= 0.8$$

## 5.6 Coefficient of Determination

$$r^2 = \text{Explained Variation} / \text{Total Variation}$$

**Example:** If  $r = 0.8$ , then  $r^2 = 0.64$  This means 64% of variation in  $y$  is explained by  $x$ .

# UNIT 6: REGRESSION ANALYSIS

## 6.1 Introduction

**Regression** is the study of the **functional relationship** between variables to **predict** one variable from the other.

### Difference from Correlation:

Correlation	Regression
Measures degree of relationship	Gives equation of relationship
Symmetric ( $r_{xy} = r_{yx}$ )	Not symmetric
No prediction	Used for prediction

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## 6.2 Lines of Regression

### Line of Regression of y on x:

(Used to predict y from x)

$$y - \bar{y} = b_{yx}(x - \bar{x})$$

or

$$y = a + b_{yx} \times x$$

### Line of Regression of x on y:

(Used to predict x from y)

$$x - \bar{x} = b_{xy}(y - \bar{y})$$

or

$$x = a' + b_{xy} \times y$$


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## 6.3 Regression Coefficients

### Regression Coefficient of y on x:

$$\begin{aligned} b_{yx} &= \frac{\sum(x - \bar{x})(y - \bar{y})}{\sum(x - \bar{x})^2} \\ &= \frac{[n\sum xy - \sum x \sum y]}{[n\sum x^2 - (\sum x)^2]} \end{aligned}$$

Also:

$$b_{yx} = r \times (\sigma_y / \sigma_x)$$

### Regression Coefficient of x on y:

$$b_{xy} = \frac{\sum(x - \bar{x})(y - \bar{y})}{\sum(y - \bar{y})^2}$$

$$= \frac{[n\sum xy - \sum x \sum y]}{[n\sum y^2 - (\sum y)^2]}$$

Also:

$$b_{xy} = r \times (\sigma_x / \sigma_y)$$

## 6.4 Properties of Regression Coefficients

1.  $r^2 = b_{yx} \times b_{xy}$      $r = \pm\sqrt{(b_{yx} \times b_{xy})}$  (Sign of  $r$  = common sign of  $b_{yx}$  and  $b_{xy}$ )
2. Both regression coefficients have the **same sign**
3. If one coefficient is  $> 1$ , the other must be  $< 1$
4. **AM of  $b_{yx}$  and  $b_{xy} \geq r$**      $(b_{yx} + b_{xy})/2 \geq r$
5. Both lines pass through the point  **$(\bar{x}, \bar{y})$**
6.  $0 \leq b_{yx} \times b_{xy} \leq 1$
7. Regression coefficients are **independent of change of origin** but **dependent on change of scale**

## 6.5 Angle between Regression Lines

$$\tan \theta = \frac{[(1-r^2) \times \sigma_x \times \sigma_y]}{[r \times (\sigma_x^2 + \sigma_y^2)]}$$

- If  $r = 0$     lines are perpendicular ( $\theta = 90^\circ$ )
- If  $r = \pm 1$     lines coincide ( $\theta = 0^\circ$ )

### Solved Example:

Given:  $n = 5$

**x** 1 2 3 4 5

**y** 2 4 5 4 5

$$\sum x = 15, \sum y = 20, \sum x^2 = 55, \sum y^2 = 86, \sum xy = 66$$

$$b_{yx} = \frac{[5(66) - 15(20)]}{[5(55) - (15)^2]}$$

$$= \frac{[330 - 300]}{[275 - 225]}$$

$$= \frac{30}{50} = 0.6$$

$$b_{xy} = \frac{[5(66) - 15(20)]}{[5(86) - (20)^2]}$$

$$= \frac{[330 - 300]}{[430 - 400]}$$

$$= \frac{30}{30} = 1.0$$

$$\bar{x} = 15/5 = 3, \bar{y} = 20/5 = 4$$

**Regression line of y on x:**

$$y - 4 = 0.6(x - 3)$$

$$y = 0.6x + 2.2$$

**Regression line of x on y:**

$$x - 3 = 1.0(y - 4)$$

$$x = y - 1$$

**Verification:**  $r = \pm\sqrt{(0.6 \times 1.0)} = \pm\sqrt{0.6} = \pm 0.775$  (positive since both b's are positive)

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## UNIT 7: PROBABILITY

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### 7.1 Basic Concepts

**Experiment:**

A process that produces well-defined outcomes.

**Random Experiment:**

An experiment whose outcome cannot be predicted with certainty.

**Sample Space (S):**

The set of all possible outcomes. **Example:** Tossing a coin  $S = \{H, T\}$  **Example:** Throwing a die  $S = \{1, 2, 3, 4, 5, 6\}$

**Event:**

A subset of the sample space.

**Types of Events:**

- **Simple Event:** Contains only one outcome
- **Compound Event:** Contains more than one outcome

- **Sure Event:** S itself (probability = 1)
  - **Impossible Event:** (probability = 0)
  - **Complementary Event:**  $A'$  or  $\bar{A}$  (everything not in A)
  - **Mutually Exclusive:**  $A \cap B = \emptyset$  (cannot occur together)
  - **Exhaustive Events:** Together they cover entire sample space
  - **Independent Events:** Occurrence of one doesn't affect other
- 

## 7.2 Definition of Probability

### Classical Definition:

$$P(A) = \frac{\text{Number of favorable outcomes}}{\text{Total number of outcomes}} \\ = \frac{n(A)}{n(S)}$$

### Properties:

1.  $0 \leq P(A) \leq 1$
  2.  $P(S) = 1$
  3.  $P(\emptyset) = 0$
  4.  $P(A') = 1 - P(A)$
- 

## 7.3 Important Counting Formulas

### Factorial:

$$n! = n \times (n-1) \times (n-2) \times \dots \times 2 \times 1 \\ 0! = 1$$

### Permutation (order matters):

$${}^n P_r = \frac{n!}{(n-r)!}$$

### Combination (order doesn't matter):

$${}^n C_r = \frac{n!}{r!(n-r)!}$$


---

## 7.4 Addition Theorem

### For two events:

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

**For mutually exclusive events ( $A \cap B = \emptyset$ ):**

$$P(A \cup B) = P(A) + P(B)$$

**For three events:**

$$P(A \cup B \cup C) = P(A) + P(B) + P(C) - P(A \cap B) - P(B \cap C) - P(A \cap C) + P(A \cap B \cap C)$$

**Solved Examples:**

**Example 1:** A card is drawn from a pack of 52 cards. Find  $P(\text{King or Heart})$ .

$$P(\text{King}) = 4/52, P(\text{Heart}) = 13/52, P(\text{King} \cap \text{Heart}) = 1/52$$

$$P(\text{King} \cup \text{Heart}) = 4/52 + 13/52 - 1/52 = 16/52 = 4/13$$

**Example 2:** Two dice are thrown. Find  $P(\text{sum} = 7)$ .

$$\text{Favorable outcomes: } (1,6),(2,5),(3,4),(4,3),(5,2),(6,1) = 6$$

$$\text{Total outcomes: } 6 \times 6 = 36$$

$$P(\text{sum}=7) = 6/36 = 1/6$$

## 7.5 Multiplication Theorem & Conditional Probability

**Conditional Probability:**

$$P(A|B) = P(A \cap B) / P(B) \quad [P(B) \neq 0]$$

**Multiplication Theorem:**

$$\begin{aligned} P(A \cap B) &= P(A) \times P(B|A) \\ &= P(B) \times P(A|B) \end{aligned}$$

**For Independent Events:**

$$P(A \cap B) = P(A) \times P(B)$$

**Solved Examples:**

**Example 1:** A bag has 5 red and 3 blue balls. Two balls are drawn without replacement. Find  $P(\text{both red})$ .

$$\begin{aligned} P(\text{1st red}) &= 5/8 \\ P(\text{2nd red} \mid \text{1st red}) &= 4/7 \\ P(\text{both red}) &= 5/8 \times 4/7 = 20/56 = 5/14 \end{aligned}$$

**Example 2:**  $P(A) = 0.4$ ,  $P(B) = 0.3$ , A and B are independent. Find  $P(A \cap B)$ .

$$P(A \cap B) = 0.4 \times 0.3 = 0.12$$

## 7.6 Bayes' Theorem

If  $B_1, B_2, \dots, B_n$  are mutually exclusive and exhaustive events, then:

$$P(B_i \mid A) = P(B_i) \times P(A \mid B_i) / \sum [P(B_j) \times P(A \mid B_j)]$$

### Solved Example:

Three machines  $M_1, M_2, M_3$  produce 30%, 45%, 25% of total items. Defective rates are 2%, 3%, 4% respectively. An item is randomly selected and found defective. Find  $P(\text{from } M_2)$ .

$$\begin{aligned} P(M_1) &= 0.30, P(M_2) = 0.45, P(M_3) = 0.25 \\ P(D \mid M_1) &= 0.02, P(D \mid M_2) = 0.03, P(D \mid M_3) = 0.04 \end{aligned}$$

$$\begin{aligned} P(D) &= 0.30(0.02) + 0.45(0.03) + 0.25(0.04) \\ &= 0.006 + 0.0135 + 0.01 \\ &= 0.0295 \end{aligned}$$

$$\begin{aligned} P(M_2 \mid D) &= P(M_2)P(D \mid M_2) / P(D) \\ &= 0.45(0.03) / 0.0295 \\ &= 0.0135 / 0.0295 \\ &= 0.4576 \approx 0.458 \end{aligned}$$

# UNIT 8: RANDOM VARIABLES & PROBABILITY DISTRIBUTIONS

## 8.1 Random Variable

A **random variable** is a function that assigns a numerical value to each outcome of a random experiment.

### Types:

1. **Discrete Random Variable:** Takes countable values (0, 1, 2, ...)
2. **Continuous Random Variable:** Takes any value in an interval

## 8.2 Probability Distribution of a Discrete RV

A table showing all possible values with their probabilities.

### Conditions:

1.  $P(x_i) \geq 0$  for all  $i$
2.  $\sum P(x_i) = 1$

### Expected Value (Mean):

$$E(X) = \mu = \sum x_i P(x_i)$$

### Variance:

$$\text{Var}(X) = \sigma^2 = E(X^2) - [E(X)]^2$$

where  $E(X^2) = \sum x_i^2 P(x_i)$

### Solved Example:

<b>X</b>	<b>0</b>	<b>1</b>	<b>2</b>	<b>3</b>
<b>P(X)</b>	0.1	0.3	0.4	0.2

$$E(X) = 0(0.1) + 1(0.3) + 2(0.4) + 3(0.2) = 0 + 0.3 + 0.8 + 0.6 = 1.7$$

$$E(X^2) = 0(0.1) + 1(0.3) + 4(0.4) + 9(0.2) = 0 + 0.3 + 1.6 + 1.8 = 3.7$$

$$\text{Var}(X) = 3.7 - (1.7)^2 = 3.7 - 2.89 = 0.81$$

$$\text{SD} = \sqrt{0.81} = 0.9$$

## 8.3 Binomial Distribution

### Conditions:

1. Fixed number of trials ( $n$ )

2. Each trial has only two outcomes (success/failure)
3. Probability of success (p) is constant
4. Trials are independent

**Formula:**

$$P(X = r) = {}^n C_r \times p^r \times q^{n-r} \quad (r = 0, 1, 2, \dots, n)$$

where  $q = 1 - p$

**Properties:**

$$\begin{aligned} \text{Mean} &= np \\ \text{Variance} &= npq \\ \text{SD} &= \sqrt{npq} \end{aligned}$$

**Important Relations:**

- Mode: If  $(n+1)p$  is integer two modes:  $(n+1)p$  and  $(n+1)p - 1$  Otherwise  $\text{Mode} = \text{floor}[(n+1)p]$
- Variance < Mean (always, since  $q < 1$ )

**Solved Example:**

A coin is tossed 5 times. Find P(exactly 3 heads).

$$n = 5, p = 1/2, q = 1/2, r = 3$$

$$\begin{aligned} P(X=3) &= {}^5 C_3 \times (1/2)^3 \times (1/2)^2 \\ &= 10 \times 1/8 \times 1/4 \\ &= 10/32 \\ &= 5/16 \\ &= 0.3125 \end{aligned}$$

$$\text{Mean} = 5 \times 0.5 = 2.5 \quad \text{Variance} = 5 \times 0.5 \times 0.5 = 1.25$$

**Another Example:**

20% of bolts are defective. From a sample of 10, find: (a) P(none defective) (b) P(exactly 2 defective) (c) Mean and Variance

$$n = 10, p = 0.2, q = 0.8$$

$$(a) P(X=0) = {}^{10} C_0 \times (0.2)^0 \times (0.8)^{10} = 1 \times 1 \times 0.1074 = 0.1074$$

$$(b) P(X=2) = {}^{10} C_2 \times (0.2)^2 \times (0.8)^8 = 45 \times 0.04 \times 0.1678 = 0.3020$$

(c) Mean =  $10(0.2) = 2$ , Variance =  $10(0.2)(0.8) = 1.6$

## 8.4 Poisson Distribution

### Conditions:

1. Events occur independently
2. Average rate ( $\lambda$ ) is constant
3. Events occur one at a time
4. Used for **rare events** (n is large, p is small)

### Formula:

$$P(X = r) = \frac{e^{-\lambda} \lambda^r}{r!} \quad (r = 0, 1, 2, \dots)$$

where  $\lambda = np = \text{mean}$

### Properties:

Mean =  $\lambda$   
 Variance =  $\lambda$   
 Mean = Variance (unique property!)  
 SD =  $\sqrt{\lambda}$

### Solved Example:

Average number of phone calls per minute = 3. Find P(exactly 5 calls in a minute).

$$\lambda = 3, r = 5$$

$$\begin{aligned} P(X=5) &= \frac{e^{-3} \times 3^5}{5!} \\ &= \frac{0.0498 \times 243}{120} \\ &= 12.10 / 120 \\ &= 0.1008 \end{aligned}$$

### Another Example:

If 2% of items are defective. Find probability that a box of 100 items contains: (a) No defective (b) At most 2 defective

$$\lambda = np = 100 \times 0.02 = 2$$

$$(a) P(X=0) = \frac{e^{-2} \times 2^0}{0!} = 0.1353$$

$$\begin{aligned}
 \text{(b) } P(X \leq 2) &= P(0) + P(1) + P(2) \\
 &= e^{-2} [2^0/0! + 2^1/1! + 2^2/2!] \\
 &= 0.1353[1 + 2 + 2] \\
 &= 0.1353 \times 5 \\
 &= 0.6767
 \end{aligned}$$

## 8.5 Normal Distribution

### Properties:

1. Continuous, bell-shaped, symmetric about mean
2. Mean = Median = Mode
3. Defined by two parameters:  $\mu$  (mean) and  $\sigma$  (standard deviation)
4. Total area under curve = 1
5. Extends from  $-\infty$  to  $+\infty$
6. Points of inflection at  $\mu \pm \sigma$

### PDF:

$$f(x) = (1/\sigma\sqrt{2\pi}) \times e^{-(x-\mu)^2/2\sigma^2} \quad (-\infty < x < \infty)$$

### Standard Normal Variable:

$$Z = (X - \mu) / \sigma$$

$Z \sim N(0, 1)$  [mean = 0, SD = 1]

### Area Properties:

$$\begin{aligned}
 P(\mu - \sigma < X < \mu + \sigma) &\approx 0.6827 \text{ (68.27\%)} \\
 P(\mu - 2\sigma < X < \mu + 2\sigma) &\approx 0.9545 \text{ (95.45\%)} \\
 P(\mu - 3\sigma < X < \mu + 3\sigma) &\approx 0.9973 \text{ (99.73\%)}
 \end{aligned}$$

### Common Z-table Values:

#### Z Area (0 to Z)

0.0	0.0000
0.5	0.1915
1.0	0.3413
1.5	0.4332
1.96	0.4750
2.0	0.4772

2.5 0.4938

3.0 0.4987

---

**Solved Example:**Marks of students are normally distributed with  $\mu = 60$ ,  $\sigma = 10$ . Find: (a)  $P(X > 75)$  (b)  $P(45 < X < 70)$ 

(a)  $Z = (75-60)/10 = 1.5$

$$P(X > 75) = P(Z > 1.5) = 0.5 - 0.4332 = 0.0668$$

(b)  $Z_1 = (45-60)/10 = -1.5$

$$Z_2 = (70-60)/10 = 1.0$$

$$P(45 < X < 70) = P(-1.5 < Z < 1.0)$$

$$= P(-1.5 < Z < 0) + P(0 < Z < 1.0)$$

$$= 0.4332 + 0.3413$$

$$= 0.7745$$

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## UNIT 9: INDEX NUMBERS

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### 9.1 Definition

An **Index Number** is a statistical measure designed to show changes in a variable or group of related variables over time, geographical location, or other characteristics.

**Base Period:** The period with which comparisons are made (index = 100) **Current Period:** The period being compared

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### 9.2 Types of Index Numbers

1. **Price Index Numbers** – Measure changes in price
  2. **Quantity Index Numbers** – Measure changes in quantity
  3. **Value Index Numbers** – Measure changes in total value
- 

### 9.3 Methods of Construction

#### A. Simple (Unweighted) Index Numbers

**1. Simple Aggregative Method:**

$$P_{01} = (\sum p_1 / \sum p_0) \times 100$$

**2. Simple Average of Relatives Method:**

Using AM:

$$P_{01} = (1/n) \times \sum (p_1/p_0 \times 100)$$

Using GM:

$$P_{01} = \text{Antilog}[(1/n) \times \sum \log(p_1/p_0 \times 100)]$$

**B. Weighted Index Numbers****1. Laspeyre's Index (Base year quantities as weights):**

$$P_{01}(L) = (\sum p_1 q_0 / \sum p_0 q_0) \times 100$$

**2. Paasche's Index (Current year quantities as weights):**

$$P_{01}(P) = (\sum p_1 q_1 / \sum p_0 q_1) \times 100$$

**3. Fisher's Index (Geometric mean of Laspeyre's and Paasche's):**

$$\begin{aligned} P_{01}(F) &= \sqrt{[P_{01}(L) \times P_{01}(P)]} \\ &= \sqrt{[(\sum p_1 q_0 / \sum p_0 q_0) \times (\sum p_1 q_1 / \sum p_0 q_1)]} \times 100 \end{aligned}$$

**4. Marshall-Edgeworth Index:**

$$P_{01}(ME) = [\sum p_1 (q_0 + q_1) / \sum p_0 (q_0 + q_1)] \times 100$$

**5. Bowley's Index:**

$$P_{01}(B) = [P_{01}(L) + P_{01}(P)] / 2$$

**6. Dorbish-Bowley Index:**

$$P_{01}(DB) = [L + P] / 2$$

**Solved Example:**

Commodity	$p_0$	$q_0$	$p_1$	$q_1$	$p_1q_0$	$p_0q_0$	$p_1q_1$	$p_0q_1$
A	10	50	12	55	600	500	660	550
B	8	30	10	35	300	240	350	280
C	5	40	6	45	240	200	270	225
<b>Total</b>					<b>1140</b>	<b>940</b>	<b>1280</b>	<b>1055</b>

Laspeyre's:  $L = (1140/940) \times 100 = 121.28$

Paasche's:  $P = (1280/1055) \times 100 = 121.33$

Fisher's:  $F = \sqrt{(121.28 \times 121.33)} = \sqrt{14714.58} = 121.30$

**9.4 Tests of Adequacy of Index Numbers****1. Time Reversal Test (TRT):**

$P_{01} \times P_{10} = 1$  (or  $100 \times 100$  if in percentages)

Method	TRT Satisfied?
Laspeyre's	No
Paasche's	No
Fisher's	Yes
Marshall-Edgeworth	Yes

**2. Factor Reversal Test (FRT):**

$P_{01} \times Q_{01} = (\sum p_1q_1 / \sum p_0q_0)$

(Price index  $\times$  Quantity index = Value ratio)

Method	FRT Satisfied?
Laspeyre's	No
Paasche's	No
Fisher's	Yes

**Fisher's Index is called "IDEAL" index number** because it satisfies both TRT and FRT.

**3. Circular Test:**

$P_{01} \times P_{12} \times P_{20} = 1$

- Satisfied by: Simple Aggregative Method

- Not satisfied by: Laspeyre's, Paasche's, Fisher's

## 9.5 Cost of Living Index (CLI) / Consumer Price Index (CPI)

### Methods:

#### A. Aggregate Expenditure Method:

$$CLI = (\sum p_1 q_0 / \sum p_0 q_0) \times 100$$

#### B. Family Budget Method (Weighted Average of Price Relatives):

$$CLI = \sum RW / \sum W$$

where  $R = (p_1/p_0) \times 100$  (Price Relative),  $W = p_0 q_0$  (Weight)

#### Solved Example (Family Budget Method):

Item	$p_0$	$p_1$	$q_0$	$R = p_1/p_0 \times 100$	$W = p_0 q_0$	$RW$
Food	20	25	10	125	200	25000
Cloth	15	18.5	120	120	75	9000
Rent	50	55	1	110	50	5500
Fuel	10	14	8	140	80	11200
<b>Total</b>					<b>405</b>	<b>50700</b>

$$CLI = 50700/405 = 125.19$$

**Interpretation:** Cost of living has increased by 25.19% compared to base period.

## 9.6 Uses of Index Numbers

1. Measure changes in price levels (inflation)
2. Measure changes in industrial/agricultural production
3. Deflating income/wage data to find real values
4. Guide for policy making
5. Dearness Allowance (DA) calculation

### Real Income:

$$Real\ Income = (Money\ Income / Price\ Index) \times 100$$

# UNIT 10: TIME SERIES ANALYSIS

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## 10.1 Definition

A **Time Series** is a set of observations recorded at successive points of time or over successive periods of time.

**Examples:** Monthly sales, yearly population, daily stock prices

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## 10.2 Components of Time Series

### 1. Secular Trend (T):

Long-term general tendency (increase or decrease)

### 2. Seasonal Variation (S):

Regular fluctuations within a year (due to seasons, festivals)

### 3. Cyclical Variation (C):

Oscillations over periods longer than a year (business cycles)

### 4. Irregular/Random Variation (I):

Unpredictable fluctuations (wars, earthquakes, pandemics)

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## 10.3 Models of Time Series

### Additive Model:

$$Y = T + S + C + I$$

### Multiplicative Model:

$$Y = T \times S \times C \times I$$

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## 10.4 Measurement of Trend

### A. Graphic/Freehand Method:

Draw a smooth curve through the plotted data points by inspection.

### B. Semi-Average Method:

1. Divide data into two equal halves
2. Calculate average of each half
3. Plot these averages at mid-points of their periods
4. Join the two points → Trend line

### C. Moving Average Method:

Calculate averages of successive groups of fixed size.

**3-year Moving Average:** Average of 3 consecutive values

**4-year Moving Average:** Requires centering (average of two consecutive 4-year averages)

**Solved Example (3-year Moving Average):**

Year	Value	3-yr Total	3-yr MA
2015	10	—	—
2016	12	10+12+14=36	12.0
2017	14	12+14+16=42	14.0
2018	16	14+16+18=48	16.0
2019	18	16+18+20=54	18.0
2020	20	—	—

### D. Method of Least Squares (Best Method)

Fit a straight line:  $Y = a + bX$

**Normal Equations:**

$$\begin{aligned}\Sigma Y &= na + b\Sigma X \\ \Sigma XY &= a\Sigma X + b\Sigma X^2\end{aligned}$$

**If origin is shifted to make  $\Sigma X = 0$ :**

$$\begin{aligned}a &= \Sigma Y/n \\ b &= \Sigma XY/\Sigma X^2\end{aligned}$$

**Solved Example:**

Year	Y	X (coding)	XY	X <sup>2</sup>
2016	10	-2	-20	4
2017	15	-1	-15	1
2018	20	0	0	0
2019	22	1	22	1
2020	28	2	56	4
<b>Total</b>	<b>95</b>	<b>0</b>	<b>43</b>	<b>10</b>

$$a = \Sigma Y/n = 95/5 = 19$$

$$b = \Sigma XY/\Sigma X^2 = 43/10 = 4.3$$

Trend Line:  $Y = 19 + 4.3X$  (Origin: 2018)

Forecast for 2021:  $X = 3$

$$Y = 19 + 4.3(3) = 19 + 12.9 = 31.9$$

## 10.5 Seasonal Variation — Ratio to Trend Method

1. Calculate trend values
2. Express original values as percentage of trend:  $(Y/T) \times 100$
3. Average these percentages for each season
4. Adjust so total = 400 (for quarterly) or 1200 (for monthly)

## 10.6 Seasonal Variation — Simple Average Method

1. Calculate average for each season (quarter/month)
2. Calculate grand average
3. Seasonal Index =  $(\text{Seasonal Average} / \text{Grand Average}) \times 100$

### Solved Example:

#### Quarter 2018 2019 2020 Average

Q1	40	42	44	42
Q2	50	52	54	52
Q3	45	48	51	48
Q4	35	38	41	38

$$\text{Grand Average} = (42+52+48+38)/4 = 180/4 = 45$$

Seasonal Index:

$$Q1 = (42/45) \times 100 = 93.33$$

$$Q2 = (52/45) \times 100 = 115.56$$

$$Q3 = (48/45) \times 100 = 106.67$$

$$Q4 = (38/45) \times 100 = 84.44$$

Total = 400

# IMPORTANT FORMULAS — QUICK REFERENCE SHEET

## Central Tendency:

$$AM = \Sigma fx / \Sigma f$$

$$GM = \text{Antilog}(\Sigma f \cdot \log x / \Sigma f)$$

$$HM = \Sigma f / \Sigma (f/x)$$

$$\text{Median} = L + [(N/2 - CF)/f] \times h$$

$$\text{Mode} = L + [(f_1 - f_0)/(2f_1 - f_0 - f_2)] \times h$$

$$\text{Mode} = 3 \text{ Median} - 2 \text{ Mean}$$

## Dispersion:

$$\text{Range} = \text{Max} - \text{Min}$$

$$QD = (Q_3 - Q_1)/2$$

$$MD = \Sigma f |x - \bar{x}| / \Sigma f$$

$$\sigma = \sqrt{[\Sigma f(x - \bar{x})^2 / \Sigma f]}$$

$$CV = (\sigma / \bar{x}) \times 100\%$$

## Correlation & Regression:

$$r = [n \Sigma xy - \Sigma x \Sigma y] / \sqrt{[n \Sigma x^2 - (\Sigma x)^2][n \Sigma y^2 - (\Sigma y)^2]}$$

$$\rho = 1 - 6 \Sigma D^2 / n(n^2 - 1)$$

$$b_{yx} = r(\sigma_y / \sigma_x)$$

$$b_{xy} = r(\sigma_x / \sigma_y)$$

$$r^2 = b_{yx} \times b_{xy}$$

## Probability:

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$
$$P(A \cap B) = P(A) \cdot P(B|A)$$
$$P(B|A) = P(B \cap A|B) / \sum P(B \cap A|B)$$

## Distributions:

Binomial:  $P(X=r) = {}^n C_r p^r q^{n-r}$ ,  $\mu=np$ ,  $\sigma^2=npq$   
Poisson:  $P(X=r) = \frac{e^{-\lambda} \lambda^r}{r!}$ ,  $\mu=\sigma^2=\lambda$   
Normal:  $Z = (X-\mu)/\sigma$

## Index Numbers:

$$L = (\sum p_1 q_0 / \sum p_0 q_0) \times 100$$
$$P = (\sum p_1 q_1 / \sum p_0 q_1) \times 100$$
$$F = \sqrt{L \times P}$$

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This covers the **complete BCA Semester 2 Statistics syllabus** with:

- All topics explained with theory
- All formulas listed
- Solved numerical examples for every topic
- Properties and important notes
- Quick revision formula sheet